

Inverse Trig Functions

Evaluate

1. $\sin^{-1}(0)$ 0
2. $\cos^{-1}0$ $\pi/2$
3. $\sin^{-1}(\frac{\sqrt{2}}{2})$ $\pi/4$
4. $\csc^{-1}(-2)$ $-\pi/6$
5. $\cos^{-1}(-\frac{\sqrt{3}}{2})$ $5\pi/6$
6. $\cos^{-1}(1)$ 0
7. $\cos^{-1}(-\frac{1}{2})$ $2\pi/3$
8. $\tan^{-1}(1)$ $\pi/4$
9. $\tan^{-1}(-1)$ $-\pi/4$
10. $\sin^{-1}(\frac{1}{2})$ $\pi/6$
11. $\cos^{-1}(-1)$ π
12. $\cos^{-1}(\frac{\sqrt{3}}{2})$ $\pi/6$
13. $\cos(\cos^{-1}(\frac{\sqrt{2}}{2}))$ $\frac{\sqrt{2}}{2}$
14. $\sin(\sin^{-1}(-\frac{\sqrt{3}}{2}))$ $-\frac{\sqrt{3}}{2}$
15. $\cos^{-1}(\cos\frac{\pi}{4})$ $\pi/4$
16. $\sin^{-1}(\sin\frac{11\pi}{6})$ $-\pi/6$
17. $\cos^{-1}(\frac{\sqrt{2}}{2})$ $\pi/4$
18. $\sin^{-1}(\cos\frac{5\pi}{6})$ $-\pi/3$
19. $\cos^{-1}(\sin\frac{3\pi}{4})$ $\pi/4$
20. $\tan^{-1}(\tan\frac{3\pi}{4})$ $-\pi/4$
21. $\cot(\tan^{-1}(\frac{1}{5}))$ 5
22. $\cos(\sin^{-1}(-\frac{2}{5}))$ $\frac{4}{5}$
23. $\sin(\cos^{-1}(-\frac{8}{9}))$ $\frac{1}{9}$
24. $\sin(\tan^{-1}(-6))$ $-\frac{6}{\sqrt{37}}$
25. $\cos(\tan^{-1}(\frac{x}{3}))$ $\frac{3}{\sqrt{x^2+9}}$
26. $\sin(\cot^{-1}(-x))$ $\frac{-x}{\sqrt{x^2+1}}$
27. $\cos(2\sin^{-1}(\frac{1}{5}))$ $\frac{23}{25}$
28. $\sin(2\cos^{-1}(\frac{4}{5}))$ $\frac{8\sqrt{33}}{49}$
29. $\sin(\tan^{-1}(\frac{2}{3}) - \sin^{-1}(\frac{5}{13}))$ $\frac{13\sqrt{13}}{9}$
30. $\cos(\sec^{-1}(-\frac{5}{3}) + \tan^{-1}(\frac{-2}{3}))$ $\frac{6}{5}$

$\cos^2 x - \sin^2 x = 2$
 $(\frac{2\sqrt{6}}{5})^2 - (\frac{1}{5})^2 = 2$
 $\frac{24}{25} - \frac{1}{25} = 2$
 $\frac{23}{25} = 2$

$\sin \alpha \cos \beta - \cos \alpha \sin \beta = \frac{24}{13\sqrt{13}} - \frac{15}{13\sqrt{13}}$
 $\frac{9}{13\sqrt{13}}$

$\cos \alpha \cos \beta - \sin \alpha \sin \beta = (\frac{-3}{5})(\frac{3}{\sqrt{13}}) - (\frac{4}{5})(\frac{-\sqrt{13}}{5})$
 $-\frac{9}{5\sqrt{13}} - \frac{-8}{5\sqrt{13}} = \frac{-1}{5\sqrt{13}}$