

## Evaluating Logarithmic Expressions

$$1) \log_2 112 - \log_2 7 = 4 \quad 2) \log_{10} 0.1^{\frac{1}{2}}$$

$$\log_2 \frac{112}{7} = x$$

$$\log_2 16 = x$$

4

$$x = \log_2 4$$

$$x = \log_2 2$$

$$x = 1$$

$$x = 1$$

$$x = 1$$

$$x = 1$$

$$\log_{10} 0.1^{\frac{1}{2}} = \frac{1}{2} \log_{10} 0.1$$

$$\frac{1}{2} \cdot \log_{10} \frac{1}{10}$$

$$\frac{1}{2} (-1)$$

$$-\frac{1}{2}$$

$$3) \log_{12} 9 + \log_{12} 16$$

$$4) e^{(3 \ln 5)} = x$$

$$\log_{12} 144$$

2

$$\ln x = 3 \ln 5$$

$$\ln x = \ln 5^3$$

$$\ln x = \ln 125$$

$$x = 125$$

Solving using Change of Base

$$1) \log_2 112$$

$$\frac{\log 112}{\log 2}$$

6.81

Change of Base formula

$$\log_b a = \frac{\log a}{\log b} = \frac{\ln a}{\ln b}$$

$$2) 3^{-x} = \sqrt{7}$$

$$\log_3 \sqrt{7} = -x$$

$$\frac{\log \sqrt{7}}{\log 3} = -x$$

$$-0.325 = -x$$

$$0.325 = x$$

$$3) (1.1)^x = 2$$

$$\log_{1.1} 2 = x$$

$$\frac{\log 2}{\log 1.1} = x$$

$$x = 7.272$$

$$4) x = \log_7 2$$

$$x = \frac{\log 2}{\log 7}$$

$$x = 0.3562$$

Solve -

$$\frac{10}{10e^x} = 2$$

$$10 = 2(10e^x)$$

$$5 = 10e^x$$

$$4 = e^x$$

$$\ln 4 = -x$$

$$-\ln 4 = x$$

$$-1.3928$$

$$\ln(\ln(10e^x))$$

$$\ln e^x = \ln 200$$

$$e^x = e^{200}$$

$$x = 200$$

$$\ln(\ln e)$$

$$e^x = e$$

$$x = 200$$

$$\ln(200)$$